## **MODERN PHYSICS**

- Work function is minimum for cesium (1.9 eV)
- \* work function W =  $hv_0 = \frac{hc}{\lambda_0}$
- Photoelectric current is directly proportional to intensity of incident radiation.
   (v constant)
- Photoelectrons ejected from metal have kinetic energies ranging from 0 to KE<sub>max</sub>

Here  $KE_{max} = eV_s$   $V_s$  - stopping potential

- Stopping potential is independent of intensity of light used (v-constant)
- Intensity in the terms of electric field is

$$I = \frac{1}{2} \in_0 E^2.c$$

- \* Momentum of one photon is  $\frac{h}{\lambda}$ .
- Einstein equation for photoelectric effect is

$$hv = w_0 + k_{max} \implies \frac{hc}{\lambda} = \frac{hc}{\lambda_0} + eV_s$$

- \* Energy  $\Delta E = \frac{12400}{\lambda(A^0)} eV$
- Force due to radiation (Photon) (no transmission)
   When light is incident perpendicularly
  - (a) a = 1 r = 0

$$F = \frac{IA}{c}$$
, Pressure =  $\frac{I}{c}$ 

(b) r = 1, a = 0

$$F = \frac{2IA}{c}$$
,  $P = \frac{2I}{c}$ 

(c) when 0 < r < 1 and a + r = 1

$$F = \frac{IA}{C} (1 + r), P = \frac{I}{C} (1 + r)$$

When light is incident at an angle  $\theta$  with vertical.

(a) 
$$a = 1, r = 0$$

$$F = \frac{IA\cos\theta}{c}$$
,  $P = \frac{F\cos\theta}{A} = \frac{I}{c}\cos 2\theta$ 

(b) 
$$r = 1, a = 0$$

$$F = \frac{2IA\cos^2\theta}{c}$$
,  $P = \frac{2I\cos^2\theta}{c}$ 

(c) 
$$0 < r < 1$$
,  $a + r = 1$ 

$$P = \frac{I\cos^2\theta}{c} (1 + r)$$

De Broglie wavelength

$$\lambda = \frac{h}{mv} = \frac{h}{P} = \frac{h}{\sqrt{2mKE}}$$

Radius and speed of electron in hydrogen like atoms.

$$r_n = \frac{n^2}{Z} a_0$$
  $a_0 = 0.529 \text{ Å}$   $v_n = \frac{Z}{n} v_0$   $v_0 = 2.19 \times 10^6 \text{ m/s}$ 

Energy in nth orbit

$$E_n = E_1 \cdot \frac{Z^2}{R^2}$$
  $E_1 = -13.6 \text{ eV}$ 

Wavelength corresponding to spectral lines

$$\frac{1}{\lambda} = R \left[ \frac{1}{n_1^2} - \frac{1}{n_2^2} \right]$$

$$n_1 = 1$$

$$n_2 = 2, 3, 4, \dots$$

$$n_1 = 2$$

$$\begin{array}{llll}
 n_1 = 1 & & & & & & \\
 n_1 = 2 & & & & & \\
 n_1 = 3 & & & & & \\
 \end{array}$$
 $\begin{array}{llll}
 n_2 = 2, 3, 4, \dots & \\
 n_2 = 3, 4, 5, \dots & \\
 n_2 = 4, 5, 6, \dots & \\
 \end{array}$ 

$$n_1 = 3$$

- The lyman series is an ultraviolet and Paschen, Brackett and Pfund series are in the infrared region.
- Total number of possible transitions, is  $\frac{n(n-1)}{2}$ , (from nth state)
- If effect of nucleus motion is considered,

$$r_n = (0.529 \text{ Å}) \frac{n^2}{Z} \cdot \frac{m}{\mu}$$

$$E_n = (-13.6 \text{ eV}) \frac{Z^2}{n^2} \cdot \frac{\mu}{m}$$

Here µ - reduced mass

$$\mu = \frac{Mm}{(M+m)}$$
, M - mass of nucleus

Minimum wavelength for x-rays

$$\lambda_{\min} = \frac{hc}{eV_0} = \frac{12400}{V_0(\text{volt})} \text{Å}$$

Moseley's Law

$$\sqrt{v} = a(z - b)$$

a and b are positive constants for one type of x-rays (independent of Z)

Average radius of nucleus may be written as

$$R = R_0 A^{1/3}$$
,  $R_0 = 1.1 \times 10^{-15} M$ 

A - mass number

- Binding energy of nucleus of mass M, is given by B =  $(ZM_p + NM_N M)C^2$
- Alpha decay process

Alpha - decay process
$${}^{A}_{Z}X \rightarrow {}^{A-4}_{z-2}Y + {}^{4}_{2}He$$
Q-value is

$$Q = \left[ m \begin{pmatrix} A \\ Z \end{pmatrix} - m \begin{pmatrix} A-4 \\ Z-2 \end{pmatrix} - m \begin{pmatrix} 4 \\ 2 \end{pmatrix} He \right] C^{2}$$

Beta-minus decay

$${}_{z}^{A}X \rightarrow {}_{z+1}^{A}Y + \beta^{-} + \nu^{-}$$

Q-value = 
$$[m(_{z}^{A}X)-m(_{Z+1}^{A}Y)]c^{2}$$

Beta plus-decay

$${}_{z}^{A}X \longrightarrow {}_{z-1}^{A}Y + \beta + + \nu$$

Q-value = 
$$[m(_{z}^{A}X)-m(_{Z-1}^{A}Y)-2me]c^{2}$$

Electron capture: when atomic electron is captured, X-rays are emitted.

$$_{z}^{A}X + e \longrightarrow _{Z-1}^{A}Y + v$$

Q-value = 
$$[m(_{z}^{A}X)-m(_{Z-1}^{A}Y)]c^{2}$$

- In radioactive decay, number of nuclei at instant t is given by  $N = N_0 e^{-\lambda t}$ , λ-decay constant.
- Activity of sample :  $A = A_0 e^{-\lambda t}$
- Activity per unit mass is called specific activity.
- Half life :  $T_{1/2} = \frac{0.693}{x}$
- Average life:  $T_{av} = \frac{T_{1/2}}{0.603}$



Page # 69

A radioactive nucleus can decay by two different processes having half lives t<sub>1</sub> and t<sub>2</sub> respectively. Effective half-life of nucleus is given by

$$\frac{1}{t} = \frac{1}{t_1} + \frac{1}{t_2}$$