

3

$A, B \Rightarrow$ symmetric matrices of same order.

$$X = AB + BA$$

$$Y = AB - BA$$

then $(XY)^T = ?$

a) XY

b) YX

c) $-YX$

d) none of these

~~$X^T = AB$~~

$$(XY)^T = Y^T \cdot X^T$$

$$= (AB - BA)^T (AB + BA)^T$$

$$= \{(AB)^T - (BA)^T\} \{(AB)^T + (BA)^T\}$$

$$= \{B^T A^T - A^T B^T\} \{B^T A^T + A^T B^T\}$$

$$\left. \begin{array}{l} A, B \text{ are symmetric matrices.} \\ \text{So } A^T = A, B^T = B \end{array} \right\}$$

$$= \{BA - AB\} \{BA + AB\}$$

$$= -(AB - BA)(AB + BA)$$

$$= -YX \text{ Ans.}$$

c) is correct.