

NOTES:-

A mathematically acceptable statement is a sentence that is either true or false.

Explained the terms: –

–Negation of a statement p:- If p denotes a statement, then the negation of p is denoted by $\sim p$.

– Compound statements and their related component statements: A statement is a compound statement if it is made up of two or smaller statements. The smaller statements are called component statements of the compound statement.

– The role of “And”, “Or”, “There exists” and “For every” in compound statements.

– The meaning of implications “If”, “only if”, “if and only if”. A sentence with if p, then q can be written in the following ways.

– p implies q (denoted by $p \Rightarrow q$)

– p is a sufficient condition for q – q is a necessary condition for p – p only if q – $\sim q$ implies $\sim p$

– The contrapositive of a statement $p \Rightarrow q$ is the statement $\sim q \Rightarrow \sim p$. The converse of a statement $p \Rightarrow q$ is the statement $q \Rightarrow p$. $p \Rightarrow q$ together with its converse, gives p if and only if q.

The following methods are used to check the validity of statements:

(i) direct method (ii) contrapositive method (iii) method of contradiction (iv) using a counter example.

De Morgons Law

1. **The complement of the union of the two sets A and B will be equal to the intersection of A' (complement of A) and B' (complement of B).** This is also known as De Morgan's Law of Union. It can be represented as $(A \cup B)' = A' \cap B'$.
2. The second law or the Law of Intersection states that **an element not in $A \cap B$ is not in A' or not in B'**. Conversely, it also states that an element not in A' or not in B' is not in $A \cap B$. i.e. $(A \cap B)$