NCERT EXEMPLAR SELECTED PROBLEMS: PROBLEM 7 ON ITF

40. If
$$\cos(\tan^{-1} x + \cot^{-1} \sqrt{3}) = 0$$
, then value of x is ______.

Sol. We have,
$$\cos(\tan^{-1} x + \cot^{-1} \sqrt{3}) = 0$$

$$\Rightarrow$$
 $\tan^{-1} x + \cot^{-1} \sqrt{3} = \cos^{-1} 0$

$$\Rightarrow \tan^{-1} x + \cot^{-1} \sqrt{3} = \frac{\pi}{2}$$

$$\Rightarrow \tan^{-1} x = \frac{\pi}{2} - \cot^{-1} \sqrt{3}$$

$$\Rightarrow \tan^{-1} x = \tan^{-1} \sqrt{3} \qquad \left(\because \tan^{-1} x + \cot^{-1} x = \frac{\pi}{2}\right)$$

$$\therefore x = \sqrt{3}$$