NCERT EXEMPLAR SELECTED PROBLEMS: PROBLEM 4 ON ITF

If $\sin^{-1}\frac{2a}{1+a^2}+\cos^{-1}\frac{1-a^2}{1+a^2}=\tan^{-1}\frac{2x}{1-x^2}$, where $a, x \in [0, 1)$ then the value of x is

(a) 0 (b)
$$\frac{a}{2}$$
 (c) a

(d)
$$\frac{2a}{1-a^2}$$

(d) We have,
$$\sin^{-1} \frac{2a}{1+a^2} + \cos^{-1} \frac{1-a^2}{1+a^2} = \tan^{-1} \frac{2x}{1-x^2}$$

$$\Rightarrow$$
 2 tan⁻¹ $a + 2 \tan^{-1} a = 2 \tan^{-1} x$

$$2 \tan^{-1} a + 2 \tan^{-1} a = 2 \tan^{-1} x$$

$$2 \tan^{-1} a + 2 \tan^{-1} a = 2 \tan^{-1} x$$

$$2 \tan^{-1} a = \sin^{-1} \frac{2x}{1 + x^2}$$

$$2 \tan^{-1} a = \tan^{-1} x$$

$$\Rightarrow \qquad 2 \tan^{-1} a = \tan^{-1} x$$

$$\Rightarrow \tan^{-1}\frac{2a}{1-a^2} = \tan^{-1}x$$

$$\Rightarrow x = \frac{2a}{1 - a^2}$$