

Qn: A value of c for which conclusion of Mean Value th^m holds for the function $f(x) = \log_e x$ on the interval $[1, 3]$ is

Sol:- Using Lagrange's Mean value th^m
let $f(x)$ be the fⁿ defined on $[a, b]$ then

$$f'(c) = \frac{f(b) - f(a)}{b - a} \quad \text{--- (1)} \\ c \in [a, b]$$

$$f(x) = \log_e x \quad \therefore f'(x) = \frac{1}{x}$$

$$\text{or } \frac{1}{c} = \frac{f(3) - f(1)}{3 - 1}$$

$$\frac{1}{c} = \frac{\log_e 3 - \log_e 1}{2} = \frac{\log_e 3}{2}$$

$$c = \frac{2}{\log_e 3} \quad \Rightarrow \quad \boxed{c = 2 \log_3 e} \quad \frac{\text{Ans}}{\text{Sol}}$$