

1.

$$2x - y + 2z = 2$$

$$x - 2y + z = -4$$

$$x + y + dz = 4$$

then the value of d such that the given system of equations has no solution, is

(a) 3

(b) 1

(c) 0

(d) -3

Sol

given system has no solutions.

$$A = \begin{bmatrix} 2 & -1 & 2 \\ 1 & -2 & 1 \\ 1 & 1 & d \end{bmatrix} \Rightarrow |A| = 0$$

$|A| = 0$ and any $|A_1|, |A_2|, |A_3|$ is non-zero.

$$\text{let } \begin{vmatrix} 2 & -1 & 2 \\ 1 & -2 & 1 \\ 1 & 1 & d \end{vmatrix} = 0 \text{ and } |A_3| = \begin{vmatrix} 2 & -1 & 2 \\ 1 & -2 & -4 \\ 1 & 1 & 4 \end{vmatrix} = 6 \neq 0$$

$$\Rightarrow 2(-2d - 1) + 1(d - 1) + 2(1 + 2) = 0$$

$$-4d - 2 + d - 1 + 6 = 0$$

$$-3d = -3$$

$$\boxed{d = 1}$$