

## Concepts

$$\textcircled{1} \quad \vec{V}_{\text{com}} = \frac{m_1 \vec{V}_1 + m_2 \vec{V}_2 + \dots + m_n \vec{V}_n}{m_1 + m_2 + \dots + m_n}$$

$$\vec{a}_{\text{com}} = \frac{m_1 \vec{a}_1 + m_2 \vec{a}_2 + \dots + m_n \vec{a}_n}{m_1 + m_2 + \dots + m_n}$$

$$\textcircled{2} \quad \vec{P} = \text{momentum}$$

$$\vec{P}_{\text{com}} = M_{\text{total}} \vec{V}_{\text{com}} = m_1 \vec{V}_1 + m_2 \vec{V}_2 + \dots + m_n \vec{V}_n$$

$$\textcircled{3} \quad \vec{F} = \frac{d\vec{P}}{dt}$$

$$\vec{F} = m \frac{d\vec{V}}{dt} + \underbrace{\vec{V} \frac{dm}{dt}}_{\substack{\text{If mass \& changes} \\ \text{with time}}}$$

$$\textcircled{4} \quad KE_{\text{total}} = \frac{1}{2} \mu (V_{\text{rel}})^2 + \frac{1}{2} M_{\text{total}} (V_{\text{com}})^2$$

$$\mu = \text{Reduced mass} = \frac{m_1 m_2}{m_1 + m_2}$$

$\frac{1}{2} \mu (V_{\text{rel}})^2$  is KE with respect to COM