

1. The questions in which two circles named S_1 and S_2 are given and we have to find the family of circles passing through the point of intersection of these two circles is-

$$S_1 + kS_2 = 0,$$

Where k is constant and k is not equal to -1 .

2. Similarly, instead of circles, there is one line $L_1 = 0$ and 1 circle $S_1 = 0$ is given then family of circle will be,

$$S_1 + kL_1 = 0,$$

Where k is constant and k is not equal to -1 .

3. In case, when circle passes through two given points (x_1, y_1) & (x_2, y_2) , the family of circle is given by:

$$(x_1 - x)(x_2 - x) + (y_1 - y)(y_2 - y) = 0$$