An observer can see through a pin-hole the top end of a thin rod of height h, placed as shown in the figure. The beaker height is 3h and its radius h. When the beaker is filled with a liquid up to a height 2h, he can see the lower end of the rod. Then the refractive index of the liquid is[2002-2 marks]

Sol-

(b) When liquid is filled in the beaker up to a height 2h, the image of the lower end A of the rod AB is formed at B so that it is visible to the eye.

$$\therefore$$
 DE = EB = 2h

$$\therefore \angle i = 45^0$$
(i)

$$\sin r = \frac{AG}{AC} = \frac{h}{h\sqrt{5}}$$

$$\left[:: AC^2 = (GC)^2 + (GA)^2 \right]$$

$$\therefore \mu = \frac{\sin i}{\sin r}$$

$$\therefore \mu = \frac{\sin i}{\sin r} \qquad \text{or} \quad \mu = \frac{\sin 45^0}{1/\sqrt{5}} \quad \text{or} \quad \mu = \sqrt{\frac{5}{2}}.$$