

QUESTION 1

If one end of a diameter of the circle $x^2 + y^2 - 4x - 6y + 11 = 0$ is $(3,4)$, then find the coordinate of the other end of the diameter.

Sol: Given equation of the circle is:

$$x^2 + y^2 - 4x - 6y + 11 = 0$$

$$\therefore 2g = -4 \text{ and } 2f = -6$$

So, the centre of the circle is $C(-g, -f) \equiv C(2, 3)$

$A(3, 4)$ is one end of the diameter.

Let the other end of the diameter be $B(x_1, y_1)$.

Here, mid point of AB is C .

$$\therefore 2 = \frac{3 + x_1}{2} \text{ and } 3 = \frac{4 + y_1}{2}$$

$$\Rightarrow x_1 = 1 \text{ and } y_1 = 2$$

So, the coordinates of other end of the diameter are $(1, 2)$

