Example 10 Find the domain of the function f given by
$$f(x) = \frac{1}{\sqrt{[x]^2 - [x] - 6}}$$

Solution Given that $f(x) = \frac{1}{\sqrt{[x]^2 - [x] - 6}}$, f is defined if $[x]^2 - [x] - 6 > 0$.
or $([x]-3)([x] + 2) > 0$,
 $\Rightarrow \qquad [x] < -2 \qquad \text{or} \qquad [x] > 3$
 $\Rightarrow \qquad x < -2 \qquad \text{or} \qquad x \ge 4$
Hence Domain $= (-\infty, -2) \cup [4, \infty)$.