

Matter waves

$f \rightarrow$ frequency $\lambda \rightarrow$ wavelength $v \rightarrow$ velocity

$$v = f \lambda$$

$$E = hf \quad ; \quad \lambda = \frac{h}{p}$$

$U = \pi c$ \rightarrow Momentum density

\downarrow
Energy density

$p \rightarrow$ momentum of photon

$$U = n h f$$

\downarrow
number density

$$\pi = n \times p = \frac{n h f}{c} = n \frac{h}{\lambda}$$

$\boxed{c = f \lambda}$

Massive particles : de broglie waves

$$n \lambda = 2d \sin \theta$$

provided we assign $\rightarrow \lambda = \frac{h}{p}$
 $p \rightarrow$ known
 \hookrightarrow associated

$p, E \rightarrow$ particle

$f, \lambda \rightarrow$ wave

$$\vec{p} = m \vec{v} \quad ; \quad E = \frac{1}{2} m v^2 = \frac{p^2}{2m}$$

$v = f \lambda \rightarrow$ Is $v_{\text{par.}}$ same as v_{wave} ? Find out (2)

$$E = hf = \frac{p^2}{2m}$$

$f \rightarrow \omega$: angular freq.

$\lambda \rightarrow k$: wave number

$$E = hf = h \frac{\omega}{2\pi} = \hbar \omega$$

$$\hbar = \frac{h}{2\pi}$$

$$\therefore \omega = 2\pi f$$

$$p = \frac{h}{\lambda} = \frac{2\pi h}{\lambda}$$

$$= \hbar \left(\frac{2\pi}{\lambda} \right) = \hbar k$$

$$k = \frac{2\pi}{\lambda}$$

$\boxed{\omega = ck} \rightarrow$ dispersion relation

$\omega = c(k') k' \rightarrow$ for different medium
different speed but same ω

matter waves

$$\lambda_m = \frac{h}{p} \quad ; \quad f_m = \frac{E}{h}$$

Non realistic case

$$E = \frac{p^2}{2m}$$

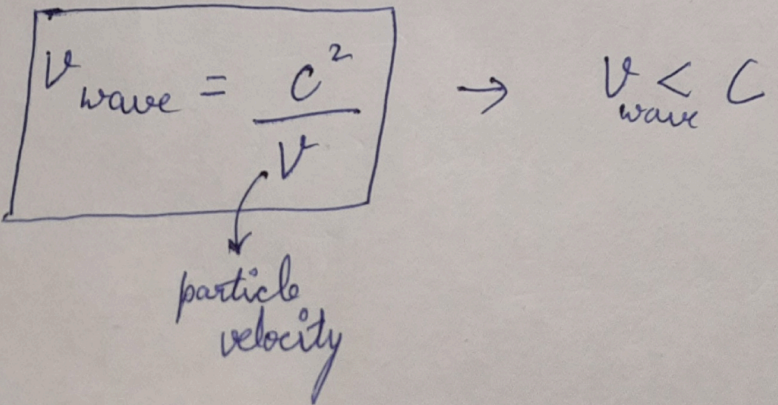
$$\lambda_m f_m = v_{\text{debroglie}} = \left(\frac{E}{p} \right)$$

$$\begin{aligned}
 v_{\text{matterwave}} &= \lambda_{mw} \omega_{mw} \\
 &= \frac{E}{p} = \frac{1}{2} \frac{mv^2}{mv} \rightarrow \text{particles velocity} \\
 &= \frac{v}{2}
 \end{aligned}$$

Relativistic Matter waves

$$E = hf \quad ; \quad p = \frac{h}{\lambda} \quad ; \quad f = \frac{E}{h} \quad ; \quad \lambda = \frac{h}{p}$$

$$\begin{aligned}
 v = \lambda f &= \frac{E}{p} \rightarrow \frac{m_0 c^2}{\sqrt{1 - v^2/c^2}} \\
 &\quad \downarrow \\
 &\quad \frac{m_0 v}{\sqrt{1 - v^2/c^2}}
 \end{aligned}$$



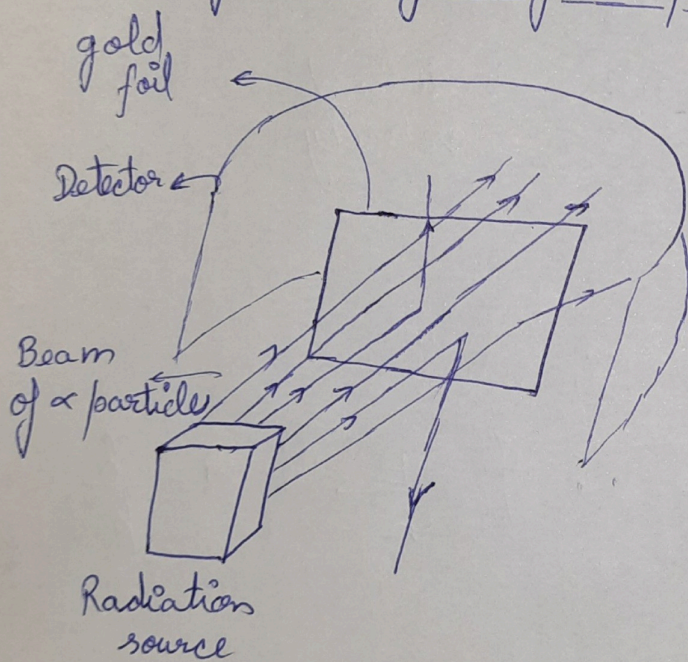
Structure of the atoms

Atoms \rightarrow fundamental units of chemical reaction

Atom's Models

- Plum pudding model \rightarrow Thompson
- Planetary model \rightarrow Rutherford
- Bohr's model

Rutherford's gold foil experiment



Observations

- 1) Most α particles travel through foil undeflected
- 2) Some particles deflect by small angles
- 3) ~~Fe~~ Very few part. deflect back from foil

Interpretation

Atom is mostly empty

Nucleus is positively charged, as is the α particle

nucleus carries most of atom's mass