

QD) Prove that $\sqrt{\frac{1-\cos x}{1+\cos x}} = \operatorname{cosec} x - \cot x$

10) RHS = $\frac{1}{\sin x} - \frac{\cos x}{\sin x} = \frac{1-\cos x}{\sin x}$

LHS = $\frac{\sqrt{1-\cos x}}{\sqrt{1+\cos x}} = \frac{\sqrt{1-\cos x} \times \sqrt{1-\cos x}}{\sqrt{1+\cos x} \sqrt{1-\cos x}}$
 $= \frac{1-\cos x}{\sin x} = \text{RHS}$

Q2) Find the value of $\cos 40^\circ - \cos 20^\circ + \cos 80^\circ$

10) $\cos 40^\circ - \cos 20^\circ + \cos 80^\circ$
 $= 2 \cos\left(\frac{40^\circ+80^\circ}{2}\right) \cos\left(\frac{40^\circ-80^\circ}{2}\right) - \cos(20^\circ)$
 $= 2 \cos(60^\circ) \cos(20^\circ) - \cos(20^\circ)$
 $= 0$

Q3) Prove that

$$\tan \theta + 2 \tan 2\theta + 4 \tan 4\theta + 8 \cot 8\theta = \cot \theta$$

10) $\tan 8\theta = \frac{2 \tan 4\theta}{1 - \tan^2 4\theta}$

$$\Rightarrow 8 \cot 8\theta + 4 \tan 4\theta = \frac{8(1 - \tan^2 4\theta) + 4 \tan(4\theta)}{2 \tan 4\theta}$$

$$= \frac{8}{2 \tan 4\theta} = \frac{4}{\tan 4\theta}$$

$$\Rightarrow \tan \theta + 2 \tan 2\theta + 4 \frac{1}{\tan 4\theta}$$

$$\therefore \tan 4\theta = \frac{2\tan 2\theta}{1-\tan^2 2\theta}$$

$$\Rightarrow \frac{2\tan 2\theta + 4}{\tan 4\theta} = \frac{2\tan 2\theta + 4(1-\tan^2 2\theta)}{2\tan 2\theta}$$

$$= \frac{2}{\tan 2\theta}$$

$$\text{Now, } \frac{\tan \theta + 2}{\tan 2\theta}$$

$$\tan 2\theta = \frac{2\tan \theta}{1-\tan^2 \theta}$$

$$\therefore \frac{\tan \theta + 2}{\tan 2\theta} = \frac{\tan \theta + \frac{2(1-\tan^2 \theta)}{2\tan \theta}}{\frac{2\tan \theta}{1-\tan^2 \theta}}$$

$$= \frac{1}{\tan \theta} = \cot \theta = \text{RHS}$$

Q3) Show that $\cos A \cos 2A \cos 4A = \frac{\sin 8A}{8 \sin A}$

A3) $\sin 8A = 2 \sin 4A \cos 4A$

$$= 4 \sin 2A \cos 2A \cos 4A$$

$$= 8 \sin A \cos A \cos 2A \cos 4A$$

$$\therefore \text{RHS} = \frac{\sin 8A}{8 \sin A} = \cos A \cos 2A \cos 4A = \text{LHS}$$