

# Important Formulae and Concepts

For a  $\triangle ABC$ ,

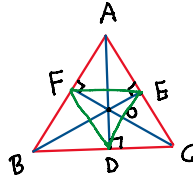
$a, b, c \rightarrow$  sides of the triangle

$A, B, C \rightarrow$  angles of the triangle

$O \rightarrow$  Orthocentre of the triangle

$D, E, F \rightarrow$  feet of the perpendiculars on sides  $BC, AC$  &  $AB$

$r, R \rightarrow$  inradius, circumradius



\* Incentre & Circumcentre of a Pedal Triangle:  $\rightarrow$

$$r' = 2R \cos A \cdot \cos B \cdot \cos C$$

$$R' = \frac{R}{2}$$

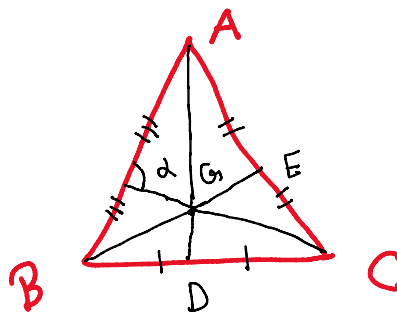
**Properties related to Median:  $\rightarrow$**

\* The line joining the mid-point of a side to the opposite vertex is called median.

\* The 3 medians of a triangle are concurrent.

\* The point of intersection of the 3 medians is called Centroid (G) of the triangle.

\* The centroid divides the median in the ratio of 2:1.



\* Length of the medians of the triangle:  $\rightarrow$

\* Length of the medians of the triangle: →

$$AD = \frac{\sqrt{2b^2 + 2c^2 - a^2}}{2}$$

$$BE = \frac{\sqrt{2a^2 + 2c^2 - b^2}}{2}$$

$$CF = \frac{\sqrt{2a^2 + 2b^2 - c^2}}{2}$$

\* Angles made by medians with the sides: →

In the above triangle,

$$\sin \alpha = \frac{2b \sin A}{\sqrt{2b^2 + 2a^2 - c^2}}$$

\* For a  $\triangle ABC$  with centroid  $G$ ,

$$\text{ar}(\triangle GAB) = \text{ar}(\triangle GBC) = \text{ar}(\triangle GCA) = \frac{1}{3} \text{ar}(\triangle ABC)$$

where  $\text{ar}(\triangle ABC)$  denotes area of  $\triangle ABC$ .

**Properties related to Ex-Centre: →**

\* The point of intersection of the angle bisectors of the exterior angles of a triangle is known as the Ex-centre.

\* There are 3 ex-centres of triangle namely  $I_1, I_2, I_3$

\*  $I_1, I_2, I_3$  form a triangle  $\triangle I_1 I_2 I_3$  called ex-central triangle.

\* Angles of Ex-Central triangle: →

$$\angle I_1 = \frac{\pi}{2} - \frac{A}{2}, \quad \angle I_2 = \frac{\pi}{2} - \frac{C}{2}, \quad \angle I_3 = \frac{\pi}{2} - \frac{B}{2}$$

where  $I_1$  is the ex-centre opposite to vertex A.

Similarly for  $I_2$  and  $I_3$ .

\* Sides of Ex-central triangle:  $\rightarrow$

$$I_1 I_2 = 4R \cos \frac{B}{2}, \quad I_2 I_3 = 4R \cos \frac{A}{2}$$

$$I_3 I_1 = 4R \cos \frac{C}{2}$$

where  $I_1$  is the ex-centre opposite to vertex A.

Similarly for  $I_2$  and  $I_3$ .

