

Example 6 Determine whether the expansion of $x^2 - \frac{2}{x}^{18}$ will contain a term containing x^{10} ?

Solution Let T_{r+1} contain x^{10} . Then

$$\begin{aligned}T_{r+1} &= {}^{18}C_r (x^2)^{18-r} \cdot \frac{-2}{x}^r \\&= {}^{18}C_r x^{36-2r} (-1)^r \cdot 2^r x^{-r} \\&= (-1)^r 2^r {}^{18}C_r x^{36-3r}\end{aligned}$$

Thus, $36 - 3r = 10$, i.e., $r = \frac{26}{3}$

