

Relations-and-Functions - Class XI

Related Questions with Solutions

Questions

Question: 01

Which one of the following is an infinite set?

- A. The set of human beings on the earth
- B. The set of water drops in a glass of water
- C. The set of trees in a forest
- D. The set of all primes

Question: 02

Consider the following statements

1. $\phi \in \{\phi\}$
2. $\{\phi\} \subseteq \phi$

Which of the statements given above is/are correct?

- A. 1 only
- B. 2 only
- C. Both 1 and 2
- D. Neither 1 nor 2

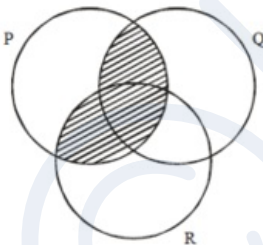
Question: 03

If $n(A) = 4$, then find number of subsets of $P(A)$.

- A. 2^4
- B. 2^8
- C. 2^{16}
- D. 2^{32}

Question: 04

What does the shaded region represent in the figure given below ?



- A. $(P \cup Q) - (P \cap Q)$
- B. $P \cap (Q \cap R)$
- C. $(P \cap Q) \cap (P \cap R)$
- D. $(P \cap Q) \cup (P \cap R)$

Question: 05

The set $A = \{x : x \in R, x^2 = 16 \text{ and } 2x = 6\}$ is

- A. Null set.
- B. Singleton set
- C. Infinite set
- D. not a well defined collection

Question: 06

If $A = \{2, 8\}$ and $B = \{3, 4, 5\}$, find number of elements in $A \times B$ and $B \times A$.

- A. 12, 12
- B. 6, 12
- C. 12, 6

D. 6, 6

Question: 07

If $A = \{2, 3, 4, 8, 10\}$, $B = \{3, 4, 5, 10, 12\}$, $C = \{4, 5, 6, 12, 14\}$ then $(A \cap B) \cup (A \cap C)$ is equal to

- A. $\{3, 4, 10\}$
- B. $\{2, 8, 10\}$
- C. $\{4, 5, 6\}$

D. $\{3, 5, 14\}$

Question: 08

If $n(A)$ denotes the number of elements in set A and if $n(A) = 4$, $n(B) = 5$ and $n(A \cap B) = 3$, then $n[(A \times B) \cap (B \times A)] =$

Solutions

Solution: 01

In the given sets, the set of all primes is an infinite set.

Solution: 02

Both statements are incorrect.

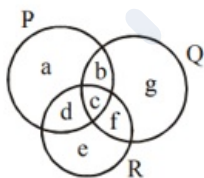
Solution: 03

$$n(A) = 4 \Rightarrow n(P(A)) = 2^4 = 16$$

Hence number of subsets of $P(A) = 2^{16}$

Solution: 04

The shaded region represents $(P \cap Q) \cup (P \cap R)$. Let the intersecting sets P, Q, R divide it into 7 regions marked, a to g as shown below.



The shaded part contains regions b, c , and d .

$$(a) (P \cup Q) - (P \cap Q) \equiv \text{regions } a, b, c, d, f, g, - (b, c)$$

$\equiv a, d, f, g$. *not correct.*

$$[b] (P \cap (Q \cap R)) \equiv a, b, c, d, \cap c, f \equiv c \text{ not correct.}$$

$$(c) (P \cap Q) \cap (P \cap R) \equiv \text{regions } b, c, \cap \text{region, } c, d \equiv c, \text{ so}$$

not correct

$$[d] (P \cap Q) \cup (P \cap R) \equiv \text{regions } b, c, \cup c, d \equiv b, c, d \text{ so correct.}$$

Solution: 05

$$A = \{x : x \in R, x^2 = 16 \text{ and } 2x = 6\}$$

$$x = 3 \text{ and } x = \pm 4$$

hence null set (no common terms)

Solution: 06

$$A = \{2, 8\}, B = \{3, 4, 5\}$$

$$A \times B = \{(2, 3), (2, 4), (2, 5), (8, 3), (8, 4), (8, 5)\} \text{ clearly } A \times B \neq B \times A$$

$$B \times A = \{(3, 2), (3, 8), (4, 2), (4, 8), (5, 2), (5, 8)\}$$

although $n(A \times B) = n(B \times A)$

Solution: 07

$$A \cap B = \{3, 4, 10\} \quad A \cap C = \{4\}$$

$$(A \cap B) \cup (A \cap C) = \{3, 4, 10\}$$

Solution: 08

$$\begin{aligned} \text{Given } n(A) &= 4, n(B) = 5, n(A \cap B) = 3 \\ n[(A \times B) \cap (B \times A)] &= n[(A \cap B) \times (B \cap A)] \\ &= n(A \cap B) \times n(B \cap A) = 3 \times 3 = 9 \quad [\because n(A \times B) = n(A) \times n(B)] \end{aligned}$$

Correct Options

Answer:01

Correct Options: D

Answer:02

Correct Options: D

Answer:03

Correct Options: C

Answer:04

Correct Options: D

Answer:05

Correct Options: A

Answer:06

Correct Options: D

Answer:07

Correct Options: A

Answer:08

Correct Answer: 9

