

Comprehension based questions-

Tangents are drawn from the point P(3, 4) to the ellipse

$$\frac{x^2}{9} + \frac{y^2}{4} = 1 \text{ touching the ellipse at points A and B.} \quad (2010)$$

6. The coordinates of A and B are

(a) (3, 0) and (0, 2)

(b) $\left(-\frac{8}{5}, \frac{2\sqrt{161}}{15}\right)$ and $\left(-\frac{9}{5}, \frac{8}{5}\right)$

(c) $\left(-\frac{8}{5}, \frac{2\sqrt{161}}{15}\right)$ and (0, 2)

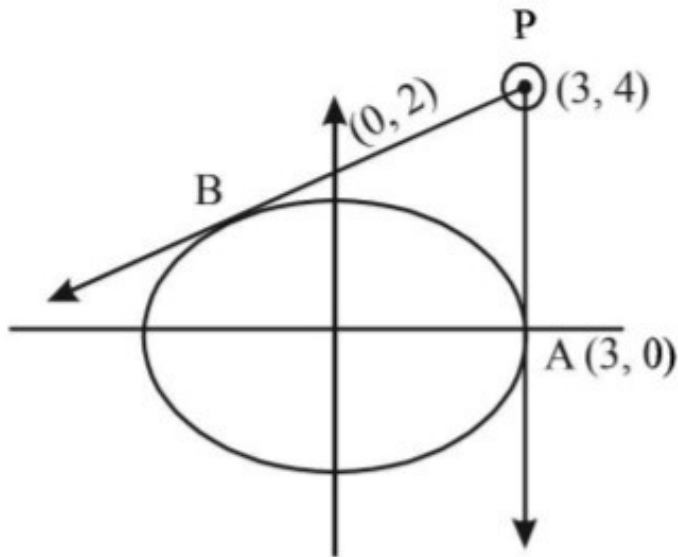
(d) (3, 0) and $\left(-\frac{9}{5}, \frac{8}{5}\right)$

7. The orthocenter of the triangle PAB is

(a) $\left(5, \frac{8}{7}\right)$ (b) $\left(\frac{7}{5}, \frac{25}{8}\right)$ (c) $\left(\frac{11}{5}, \frac{8}{5}\right)$ (d) $\left(\frac{8}{25}, \frac{7}{5}\right)$

Solution: -

6. (d) Tangent to $\frac{x^2}{3^2} + \frac{y^2}{2^2} = 1$ at the point $(3 \cos \theta, 2 \sin \theta)$ is
- $$\frac{x \cos \theta}{3} + \frac{y \sin \theta}{2} = 1$$



As it passes through $(3, 4)$, we get

$$\cos \theta + 2 \sin \theta = 1$$

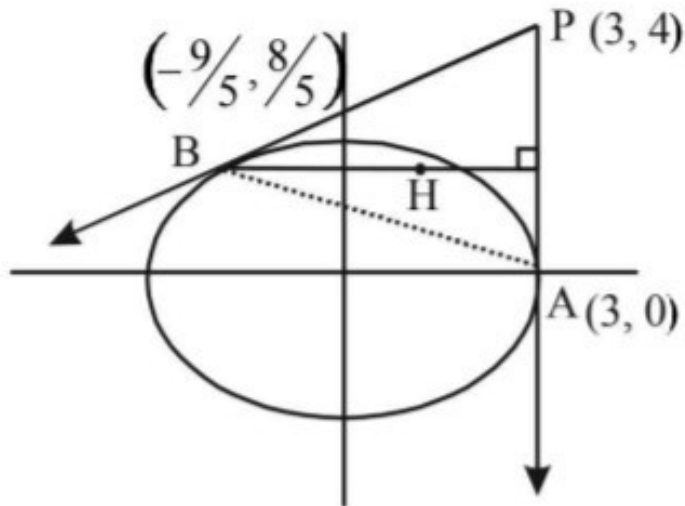
$$\Rightarrow 4 \sin^2 \theta = 1 + \cos^2 \theta - 2 \cos \theta$$

$$\Rightarrow 5 \cos^2 \theta - 2 \cos \theta - 3 = 0$$

$$\Rightarrow \cos \theta = 1, -\frac{3}{5} \Rightarrow \sin \theta = 0, \frac{4}{5}$$

\therefore Required points are A $(3, 0)$ and B $\left(-\frac{9}{5}, \frac{8}{5}\right)$

7. (c) Let H be the orthocentre of $\triangle PAB$, then as $BH \perp AP$, BH is a horizontal line through B.



\therefore y- coordinate of B = $8/5$

Let H has coordinator $(\alpha, 8/5)$

$$\text{Then slope of PH} = \frac{\frac{8}{5} - 4}{\alpha - 3} = \frac{-12}{5(\alpha - 3)}$$

$$\text{and slope of AB} = \frac{\frac{8}{5} - 0}{-\frac{9}{5} - 3} = \frac{8}{-24} = \frac{-1}{3}$$