

substance by one degree celsius (or one kelvin). For finding out the heat,  $q$ , required to raise the temperatures of a sample, we multiply the specific heat of the substance,  $c$ , by the mass  $m$ , and temperatures change,  $\Delta T$  as

$$q = c \times m \times \Delta T = C \Delta T \quad (6.11)$$

#### (d) The Relationship between $C_p$ and $C_v$ for an Ideal Gas

At constant volume, the heat capacity,  $C$  is denoted by  $C_v$  and at constant pressure, this is denoted by  $C_p$ . Let us find the relationship between the two.

We can write equation for heat,  $q$

at constant volume as  $q_v = C_v \Delta T = \Delta U$

at constant pressure as  $q_p = C_p \Delta T = \Delta H$

The difference between  $C_p$  and  $C_v$  can be derived for an ideal gas as:

$$\begin{aligned} \text{For a mole of an ideal gas, } \Delta H &= \Delta U + \Delta(pV) \\ &= \Delta U + \Delta(RT) \\ &= \Delta U + R\Delta T \end{aligned}$$

$$\therefore \Delta H = \Delta U + R\Delta T \quad (6.12)$$

On putting the values of  $\Delta H$  and  $\Delta U$ , we have

$$C_p \Delta T = C_v \Delta T + R\Delta T$$

$$C_p = C_v + R$$

$$C_p - C_v = R \quad (6.13)$$

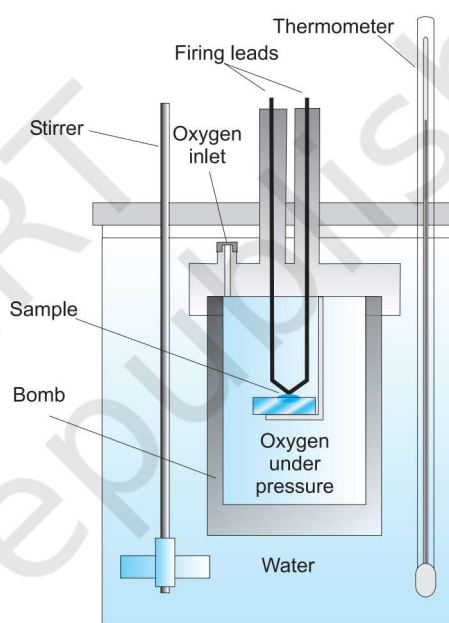
### 6.3 MEASUREMENT OF $\Delta U$ AND $\Delta H$ : CALORIMETRY

We can measure energy changes associated with chemical or physical processes by an experimental technique called calorimetry. In calorimetry, the process is carried out in a vessel called calorimeter, which is immersed in a known volume of a liquid. Knowing the heat capacity of the liquid in which calorimeter is immersed and the heat capacity of calorimeter, it is possible to determine the heat evolved in the process by measuring temperature changes. Measurements are made under two different conditions:

- i) at constant volume,  $q_v$
- ii) at constant pressure,  $q_p$

#### (a) $\Delta U$ Measurements

For chemical reactions, heat absorbed at constant volume, is measured in a bomb calorimeter (Fig. 6.7). Here, a steel vessel (the bomb) is immersed in a water bath. The whole device is called calorimeter. The steel vessel is immersed in water bath to ensure that no heat is lost to the surroundings. A combustible substance is burnt in pure dioxygen supplied



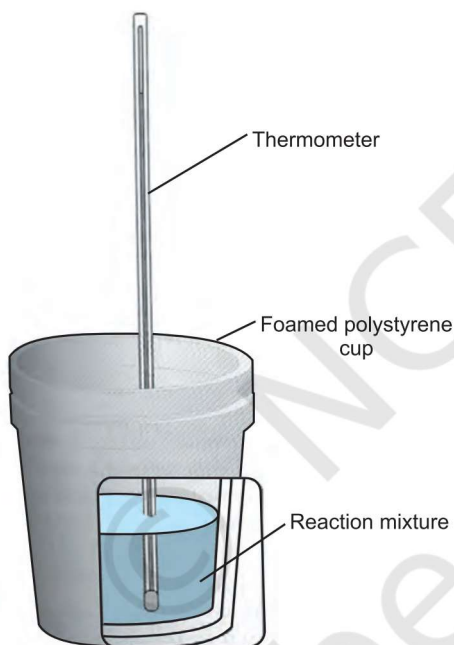
**Fig. 6.7** Bomb calorimeter

in the steel bomb. Heat evolved during the reaction is transferred to the water around the bomb and its temperature is monitored. Since the bomb calorimeter is sealed, its volume does not change i.e., the energy changes associated with reactions are measured at constant volume. Under these conditions, no work is done as the reaction is carried out at constant volume in the bomb calorimeter. Even for reactions involving gases, there is no work done as  $\Delta V = 0$ . Temperature change of the calorimeter produced by the completed reaction is then converted to  $q_v$ , by using the known heat capacity of the calorimeter with the help of equation 6.11.

**(b)  $\Delta H$  Measurements**

Measurement of heat change at constant pressure (generally under atmospheric pressure) can be done in a calorimeter shown in Fig. 6.8. We know that  $\Delta H = q_p$  (at constant  $p$ ) and, therefore, heat absorbed or evolved,  $q_p$  at constant pressure is also called the heat of reaction or enthalpy of reaction,  $\Delta_r H$ .

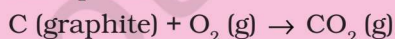
In an exothermic reaction, heat is evolved, and system loses heat to the surroundings. Therefore,  $q_p$  will be negative and  $\Delta_r H$  will also be negative. Similarly in an endothermic reaction, heat is absorbed,  $q_p$  is positive and  $\Delta_r H$  will be positive.



**Fig. 6.8** Calorimeter for measuring heat changes at constant pressure (atmospheric pressure).

**Problem 6.6**

1g of graphite is burnt in a bomb calorimeter in excess of oxygen at 298 K and 1 atmospheric pressure according to the equation



During the reaction, temperature rises from 298 K to 299 K. If the heat capacity

of the bomb calorimeter is 20.7 kJ/K, what is the enthalpy change for the above reaction at 298 K and 1 atm?

**Solution**

Suppose  $q$  is the quantity of heat from the reaction mixture and  $C_v$  is the heat capacity of the calorimeter, then the quantity of heat absorbed by the calorimeter.

$$q = C_v \times \Delta T$$

Quantity of heat from the reaction will have the same magnitude but opposite sign because the heat lost by the system (reaction mixture) is equal to the heat gained by the calorimeter.

$$q = -C_v \times \Delta T = -20.7 \text{ kJ/K} \times (299 - 298) \text{ K} \\ = -20.7 \text{ kJ}$$

(Here, negative sign indicates the exothermic nature of the reaction)

Thus,  $\Delta U$  for the combustion of the 1g of graphite =  $-20.7 \text{ kJ K}^{-1}$

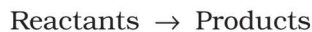
For combustion of 1 mol of graphite,

$$= \frac{12.0 \text{ g mol}^{-1} \times (-20.7 \text{ kJ})}{1 \text{ g}}$$

$$= -2.48 \times 10^2 \text{ kJ mol}^{-1}, \quad \text{Since } \Delta n_g = 0, \\ \Delta H = \Delta U = -2.48 \times 10^2 \text{ kJ mol}^{-1}$$

**6.4 ENTHALPY CHANGE,  $\Delta_r H$  OF A REACTION – REACTION ENTHALPY**

In a chemical reaction, reactants are converted into products and is represented by,



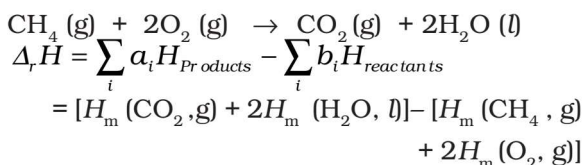
The enthalpy change accompanying a reaction is called the **reaction enthalpy**. The enthalpy change of a chemical reaction, is given by the symbol  $\Delta_r H$

$$\Delta_r H = (\text{sum of enthalpies of products}) - (\text{sum of enthalpies of reactants})$$

$$= \sum_i a_i H_{\text{products}} - \sum_i b_i H_{\text{reactants}} \quad (6.14)$$

Here symbol  $\sum$  (sigma) is used for summation and  $a_i$  and  $b_i$  are the stoichiometric

coefficients of the products and reactants respectively in the balanced chemical equation. For example, for the reaction



where  $H_m$  is the molar enthalpy.

Enthalpy change is a very useful quantity. Knowledge of this quantity is required when one needs to plan the heating or cooling required to maintain an industrial chemical reaction at constant temperature. It is also required to calculate temperature dependence of equilibrium constant.

#### (a) Standard Enthalpy of Reactions

Enthalpy of a reaction depends on the conditions under which a reaction is carried out. It is, therefore, necessary that we must specify some standard conditions. **The standard enthalpy of reaction is the enthalpy change for a reaction when all the participating substances are in their standard states.**

**The standard state of a substance at a specified temperature is its pure form at 1 bar.** For example, the standard state of liquid

ethanol at 298 K is pure liquid ethanol at 1 bar; standard state of solid iron at 500 K is pure iron at 1 bar. Usually data are taken at 298 K.

Standard conditions are denoted by adding the superscript  $\ominus$  to the symbol  $\Delta H$ , e.g.,  $\Delta H^\ominus$

#### (b) Enthalpy Changes during Phase Transformations

Phase transformations also involve energy changes. Ice, for example, requires heat for melting. Normally this melting takes place at constant pressure (atmospheric pressure) and during phase change, temperature remains constant (at 273 K).



Here  $\Delta_{\text{fus}} H^\ominus$  is enthalpy of fusion in standard state. If water freezes, then process is reversed and equal amount of heat is given off to the surroundings.

**The enthalpy change that accompanies melting of one mole of a solid substance in standard state is called standard enthalpy of fusion or molar enthalpy of fusion,  $\Delta_{\text{fus}} H^\ominus$ .**

Melting of a solid is endothermic, so all enthalpies of fusion are positive. Water requires

**Table 6.1 Standard Enthalpy Changes of Fusion and Vaporisation**

Substance	$T_f/\text{K}$	$\Delta_{\text{fus}} H^\ominus/(\text{kJ mol}^{-1})$	$T_b/\text{K}$	$\Delta_{\text{vap}} H^\ominus/(\text{kJ mol}^{-1})$
$\text{N}_2$	63.15	0.72	77.35	5.59
$\text{NH}_3$	195.40	5.65	239.73	23.35
HCl	159.0	1.992	188.0	16.15
CO	68.0	6.836	82.0	6.04
$\text{CH}_3\text{COCH}_3$	177.8	5.72	329.4	29.1
$\text{CCl}_4$	250.16	2.5	349.69	30.0
$\text{H}_2\text{O}$	273.15	6.01	373.15	40.79
NaCl	1081.0	28.8	1665.0	170.0
$\text{C}_6\text{H}_6$	278.65	9.83	353.25	30.8

( $T_f$  and  $T_b$  are melting and boiling points, respectively)