

## **Practice Questions**

Q1.

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**Example 6** Prove that  $(A^{-1})' = (A')^{-1}$ , where A is an invertible matrix.

**Solution** Since A is an invertible matrix, so it is non-singular.

We know that |A| = |A'|. But  $|A| \neq 0$ . So  $|A'| \neq 0$  i.e. A' is invertible matrix.

Now we know that  $AA^{-1} = A^{-1} A = I$ .

Taking transpose on both sides, we get  $(A^{-1})'$   $A' = A' (A^{-1})' = (I)' = I$ 

Hence  $(A^{-1})'$  is inverse of A', i.e.,  $(A')^{-1} = (A^{-1})'$ 

Q2.

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Example 17 If 
$$A = \begin{bmatrix} x & 5 & 2 \\ 2 & y & 3 \\ 1 & 1 & z \end{bmatrix}$$
,  $xyz = 80$ ,  $3x + 2y + 10z = 20$ , then
$$A \ adj. A = \begin{bmatrix} 81 & 0 & 0 \\ 0 & 81 & 0 \\ 0 & 0 & 81 \end{bmatrix}.$$

$$A \ adj. \ A = \begin{bmatrix} 81 & 0 & 0 \\ 0 & 81 & 0 \\ 0 & 0 & 81 \end{bmatrix}$$

**Solution**: False.

Q3.

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- 34. If A and B are invertible matrices, then which of the following is not correct?
  - (a) adj.  $A = |A| \cdot A^{-1}$ (c)  $(AB)^{-1} = B^{-1}A^{-1}$

(b)  $\det(A)^{-1} = [\det(A)]^{-1}$ (d)  $(A + B)^{-1} = B^{-1} + A^{-1}$ 

Sol. (d) Given A and B are invertible matrices.

Now 
$$(AB)B^{-1}A^{-1}$$
  
 $= A(BB^{-1})A^{-1} = AIA^{-1} = (AI)A^{-1} = AA^{-1} = I$   
 $\Rightarrow (AB)^{-1} = B^{-1}A^{-1}$   
Also  $AA^{-1} = I$   
 $\Rightarrow |AA^{-1}| = |I|$   
 $\Rightarrow |A||A^{-1}| = 1$   
 $\Rightarrow |A^{-1}| = \frac{1}{|A|}$   
 $\Rightarrow \det(A)^{-1} = [\det(A)]^{-1}$   
Also we know that  $A^{-1} = \frac{\text{adj. } A}{|A|}$ 

Also we know that 
$$A^{-1} = \frac{\text{adj. } A}{|A|}$$

⇒ adj. 
$$A = |A| \cdot A^{-1}$$
  
 $(A+B)^{-1} = \frac{1}{|A+B|} \text{adj.} (A+B)$   
But  $B^{-1} + A^{-1} = \frac{1}{|B|} \text{adj.} B + \frac{1}{|A|} \text{adj.} A$   
⇒  $(A+B)^{-1} \neq B^{-1} + A^{-1}$ 

Q4.

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- **49.**  $(aA)^{-1} = \frac{1}{a}A^{-1}$ , where a is any real number and A is a square matrix.
- Sol. False

Since, we know that, if A is a non-singular square matrix, then for any scalar a (non-zero), aA is invertible such that

$$(aA)\left(\frac{1}{a}A^{-1}\right) = \left(a \cdot \frac{1}{z}\right)(A \cdot A^{-1}) = I$$

i.e,  $\left(\frac{1}{a}A^{-1}\right)$  is inverse of (aA).

or  $(aA)^{-1} = \frac{1}{a}A^{-1}$ , where a is any non-zero scalar.

In the above statement it is not given that A is non-singular matrix. Hence, statement is false.



**50.**  $|A^{-1}| \neq |A|^{-1}$ , where A is non-singular matrix.

Sol. False

We know that  $|A^{-1}| = |A|^{-1}$ , where A is a non-singular matrix.

51. If A and B are matrices of order 3 and |A| = 5, |B| = 3, then  $|3AB| = 27 \times 5 \times 3 = 405$ .

Sol. True.

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We know that,  $|AB| = |A| \cdot |B|$  and  $|kA| = k^n |A|$ , where k is scalar and n is order of matrix A

$$|3AB| = 3^3 |AB| = 27|A| \cdot |B| = 27 \times 5 \times 3 = 405$$

52. If the value of a third order determinant is 12, then the value of the determinant formed by replacing each element by its co-factor will be 144.

Sol. True

Let A is the determinant.

Given |A| = 12

Also, we know that, if A is a square matrix of order n, then  $|adj A| = |A|^{n-1}$ . For n = 3,  $|adj A| = |A|^{3-1} = |A|^2 = (12)^2 = 144$